

Nuclear Technology

Radioactivity Calculations

Example 1

- α – particles ionise 95 000 atoms per cm of air.
- α – particles lose 42 eV per ionised atom
- Q1. How much energy (Joules) will α – particles lose per cm of air ?
- Q2. How far does α – particles travel before it loses 4.8 MeV of energy ?

Answer 1

- Q1. 95 000 atoms per cm. 42 eV per atom.
- $95\,000 \times 42 = 3.99 \text{ MeV per cm of air}$
- $1 \text{ eV} = 1.6 \times 10^{-19} \text{ Joules (J)}$
- $(3.99 \times 10^6) \times (1.6 \times 10^{-19}) = 6.384 \times 10^{-13} \text{ J}$
- $4.8 \text{ MeV} = 4.8 \times 10^6 \text{ eV}$
- $(4.8 \times 10^6)/42 = 114\,285 \text{ atoms}$
- $114\,285/95\,000 = 1.20 \text{ cm of air}$

Example 2

- Bi-214 has $T_{1/2} = 19.7$ min. Bi-214 is an active component in a new medical technique for treating lung cancer.
- The patient requires 22 mg of Bi-214 and the delivery time is 5 hours from the Lucas Height Nuclear Reactor to Royal Perth Hospital.
- How much Bi-214 is in the original sample produced at Nuclear Reactor ?

Answer 2

- Use $N_t = N_o(1/2)^{t/T_{1/2}}$
- $22 \times 10^{-3} = N_o(1/2)^{300/19.7}$
- $22 \times 10^{-3} = N_o(2.61 \times 10^{-5})$
- $N_o = (22 \times 10^{-3}) / (2.61 \times 10^{-5})$
- $N_o = 844.57 \text{ g}$

Example 3

- An isotope decays over an unknown time with an initial mass of 1.23 g and final mass of 0.087 g. The isotope has a half-life of 9.8 years.
- What was the length of decay for isotope ?

Answer 3

- $N=N_0(1/2)^{t/T_{1/2}}$ Let $X = t/(T_{1/2})$
- $0.087 = 1.23 \times (1/2)^X$
- $\text{Log}(0.087/1.23) = X\text{log}(1/2)$
- $-1.1504 = X(-0.3010)$
- $X = 1.1504/0.3010$
- $X = 3.822$ half lives or $X = t/(T_{1/2}) = t/9.8$
- $t = 3.822 \times 9.8 = 37.5$ years

Example 4

- A woman receives $300\mu\text{Sv}$ for a pelvic X-ray. The woman weighs 76 kg and undergoes medical treatment using a radioactive isotope that emits α -particles.
- The α -decay exposes $300\mu\text{Sv}$ of radiation to patient.
- Compare the energy difference between the pelvic X-ray and the radioactive isotope ?

Answer 4

- Dose equivalent (DE) = Absorbed dose (AD) x Quality factor (QF)
- X-ray: $300 \times 10^{-6} \text{ Sv} = \text{AD} \times 1$
- $\text{AD} = \text{Energy}/\text{Mass}$
- $\text{Energy} = (300 \times 10^{-6}) \times (76)$
- $\text{Energy} = 0.0228 \text{ or } 2.28 \times 10^{-2} \text{ J}$
- $\alpha\text{-decay} = 300 \times 10^{-6} = \text{AD} \times 20$
- $\text{AD} = (300 \times 10^{-6})/20 = 1.5 \times 10^{-5}$
- $\text{Energy} = (1.5 \times 10^{-5}) \times (76) = 1.14 \times 10^{-3} \text{ J}$
- Thus energy of X-ray > α -decay

Example 5

A Lethal Dose that kills $X\%$ of exposed people in a specific time period can be summarised by this example $LD_{50/20} = 3Sv$. This indicates that $3Sv$ of a specific radiation is a lethal dose that kills 50% of exposed people in 20 days.

Question

- An X-ray technician receives a dangerous dose of radiation of 100 mSv. A warning label on the X-ray equipment states $LD_{80/15} = 2.5 \text{ Sv}$.
- How many similar doses of radiation can the technician absorb before it reaches the limit ?
- How many days of exposure to radiation before a lethal dose ?
- What is the chance that technician will not die from lethal dose ?

Answer 5

- $2.5 \text{ Sv}/100 \text{ mSv} = 2.5/(100 \times 10^{-3})$
- = 25 doses
- 15 days for exposure to radiation
- Lethal dose at 2.5 Sv over 15 days at 80% chance
- 20% chance that technician will not die