

**[...] you refer to a result from L2 that you can determine in linear time whether something folds flat. Is this referring to the mingling algorithm? I haven't thought about this in detail, but it appears to take something like quadratic time [...]**

**I was a tad confused on the local foldability algorithm. An example in class actually running the algorithm would probably clear it up.**

**Can you clarify what you mean by a path or cycle?**

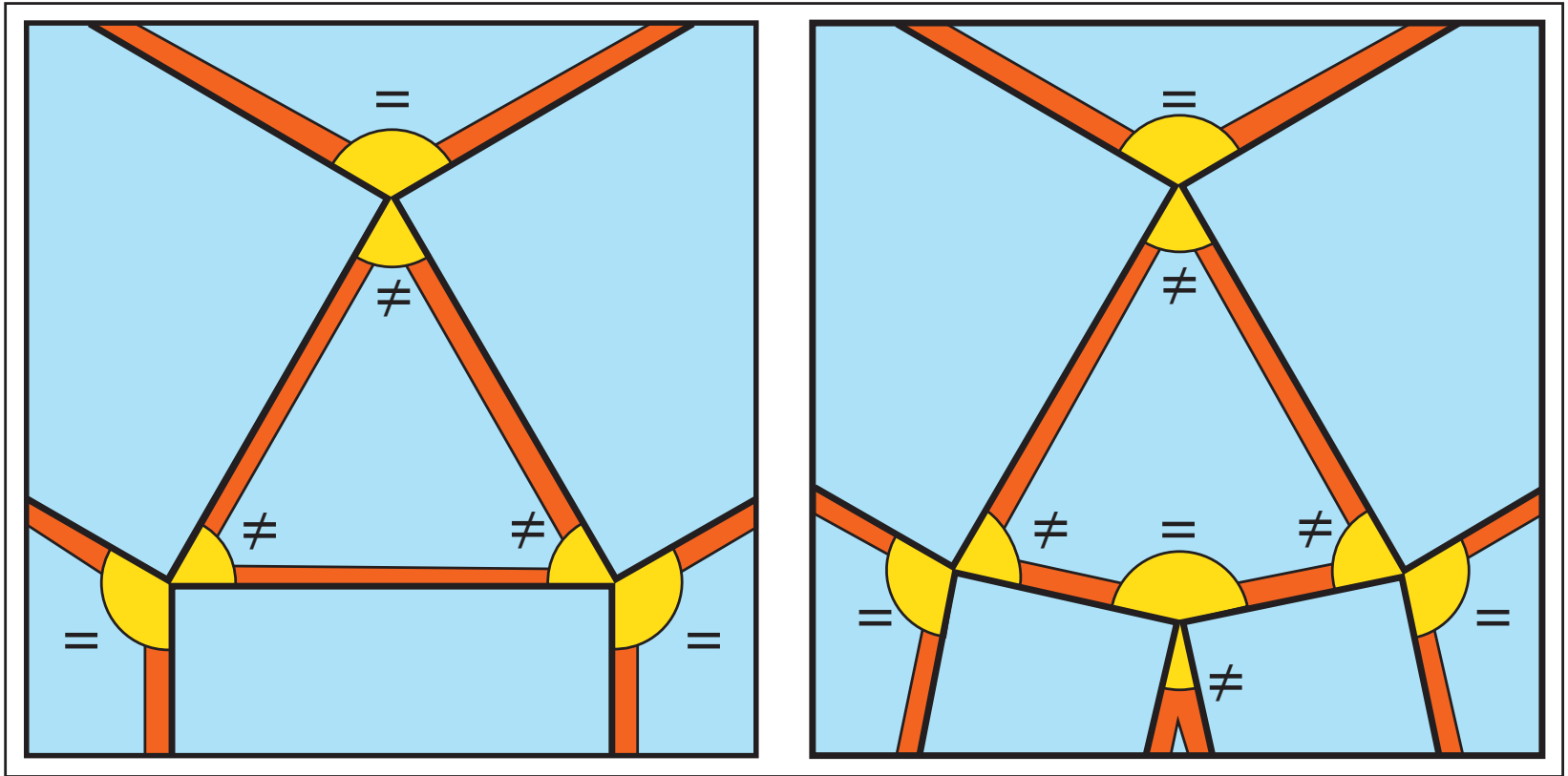
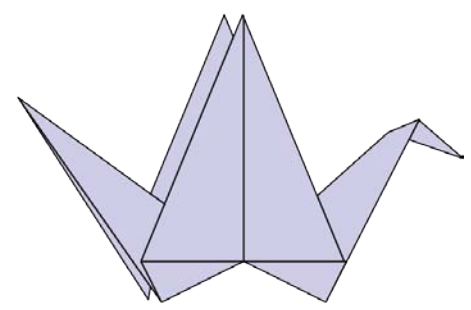
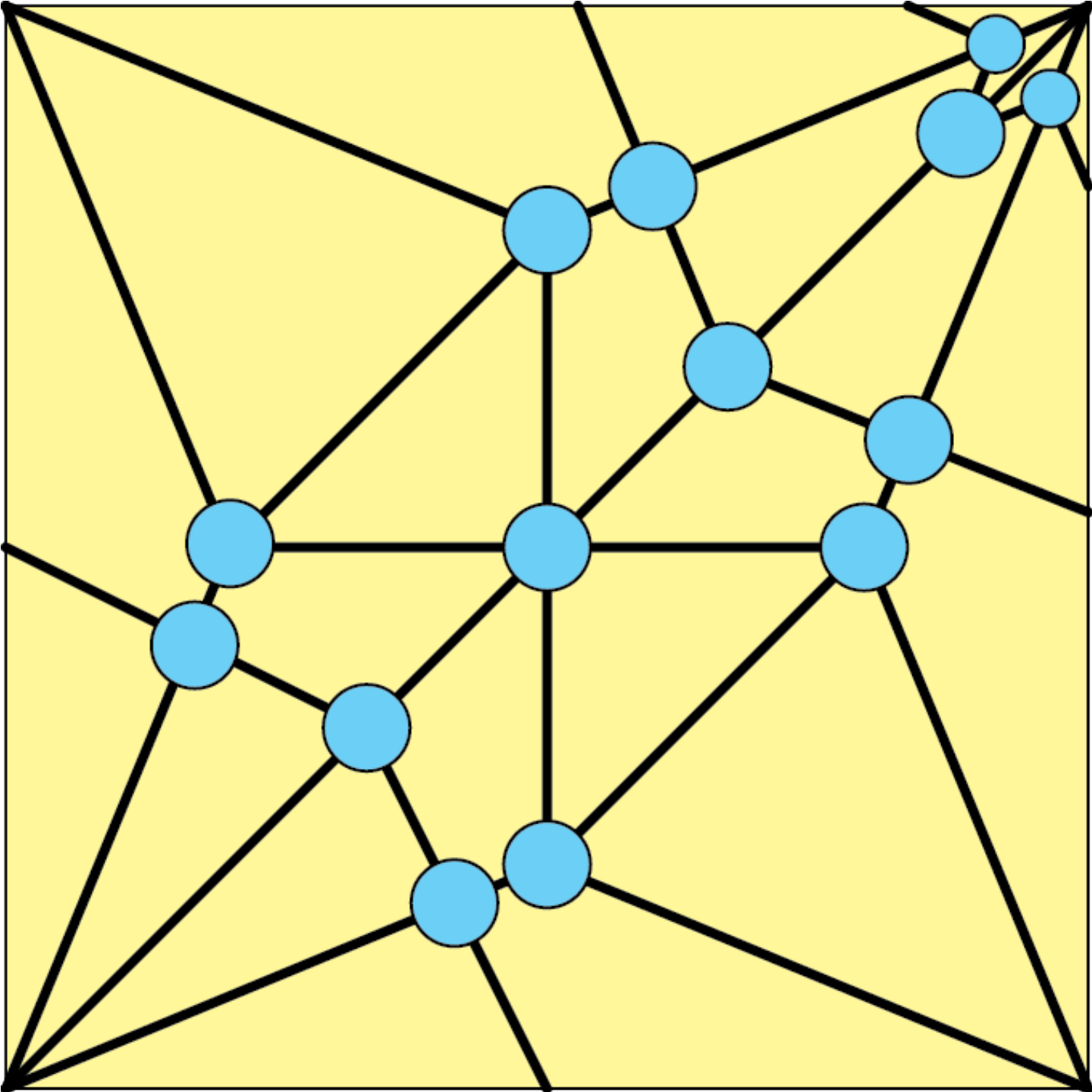
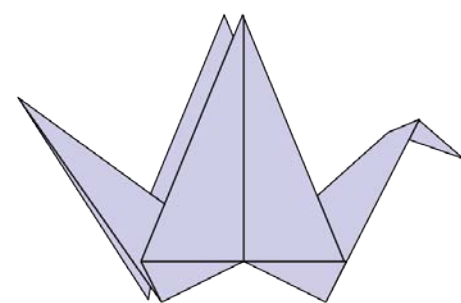
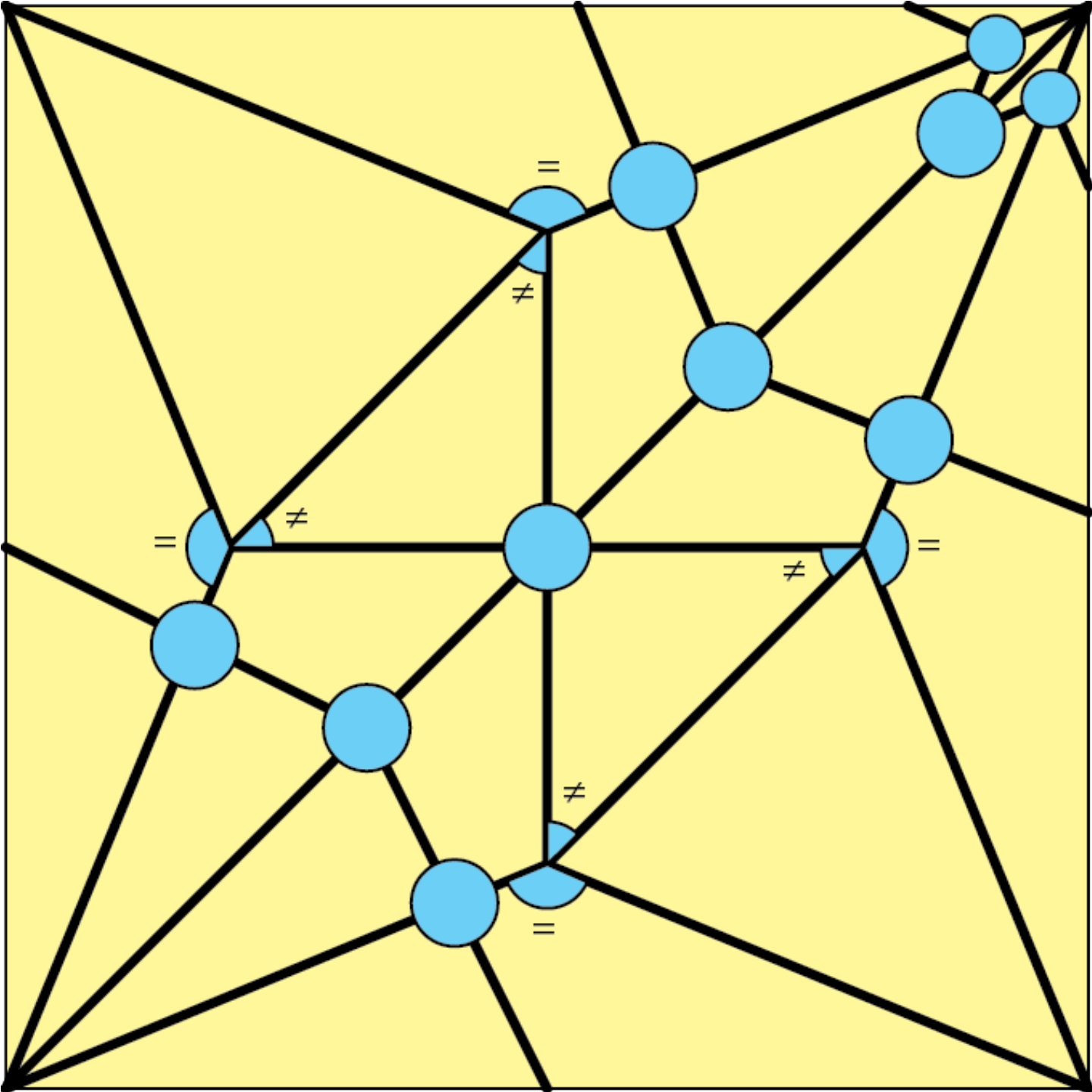
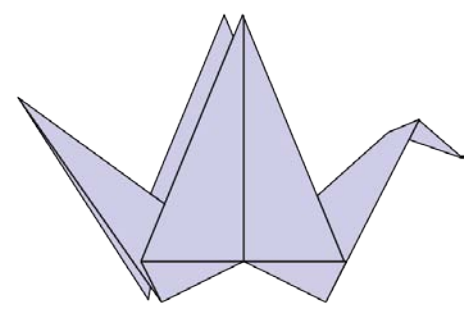
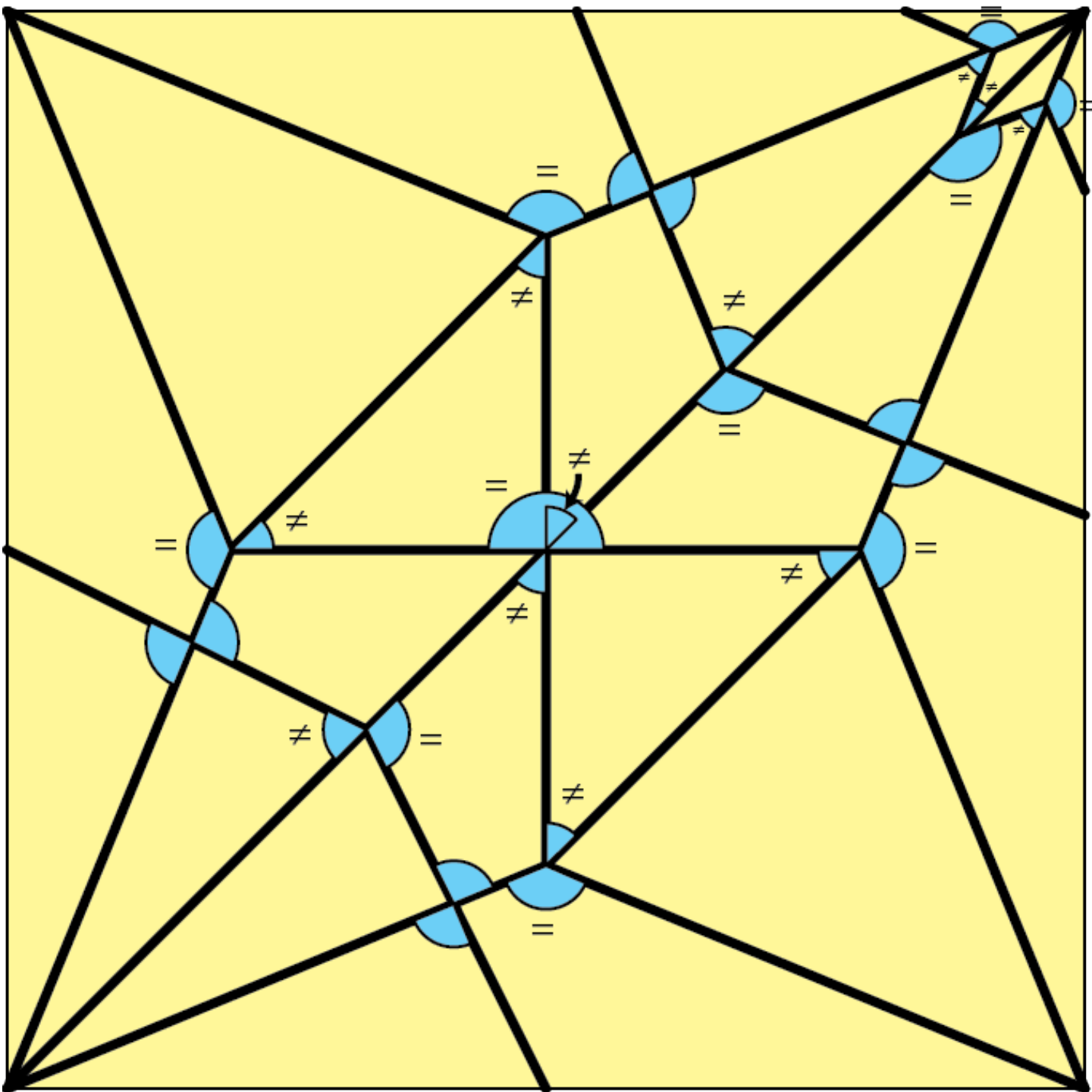
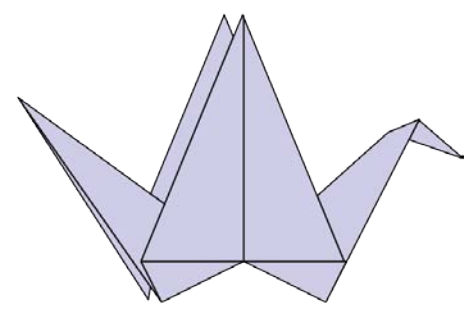
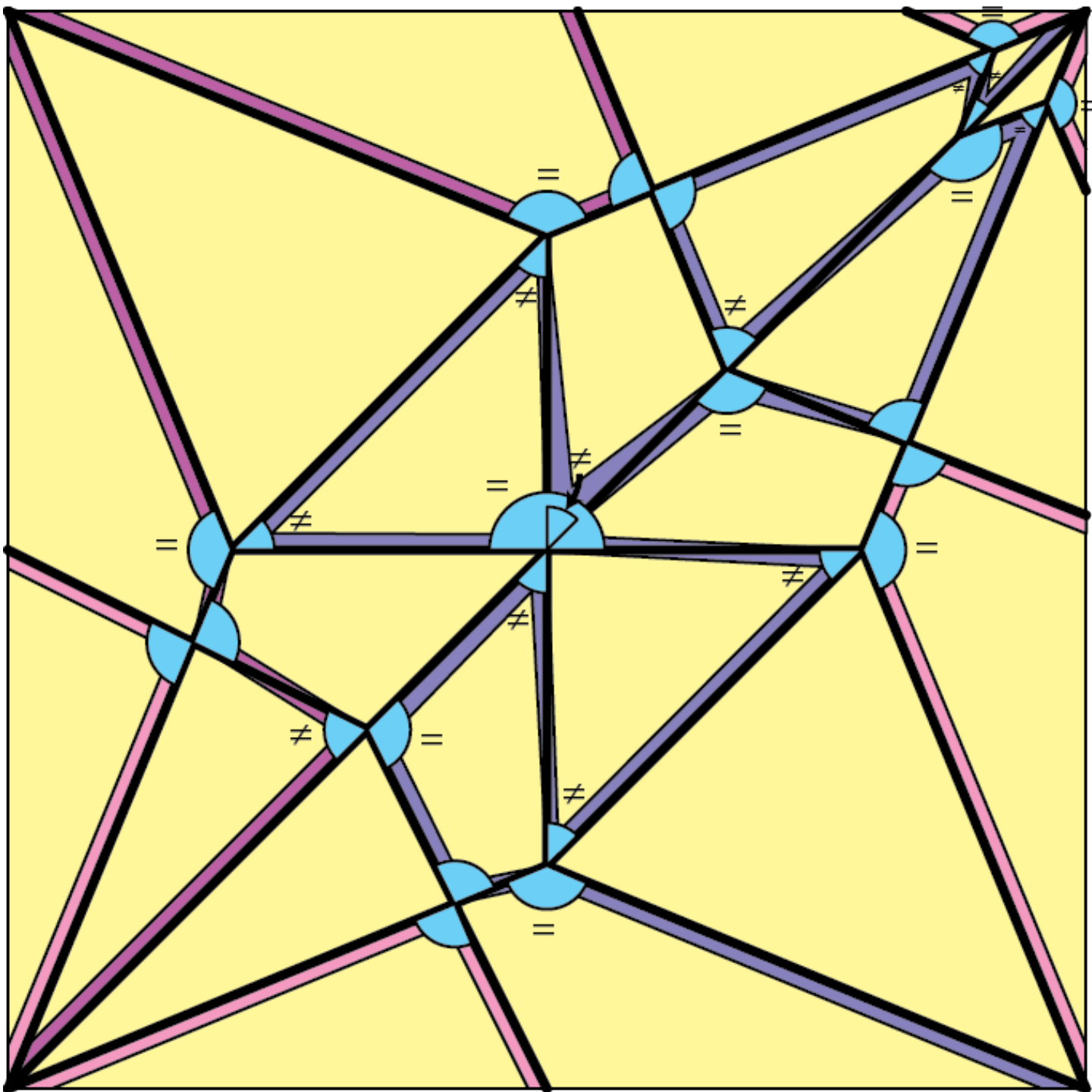


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**>360° cones could be made by fabric — perhaps you want to fold a garment along its seams, but the seamed sections meet in a point and the sum of the angles is greater than 360° (e.g., underarm of a shirt)**



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**If flat foldability is to fold a 2D sheet of paper in 2 dimensions, are there results for “flat foldability” in higher dimensions, i.e. to fold a  $d$ -dimensional sheet of paper in  $d$  dimensions? Can the result be generalized to higher dimensions?**

Images removed due to copyright restrictions.

Refer to: Kawasaki, Toshikazu. "On High Dimensional Flat Origamis." *Proceedings of the First International Meeting of Origami Science and Technology* (1989): 131–41.

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## 1.2. Flat origamis of $\mathbf{R}^3$

**Definition 1.2 (flat origamis of  $\mathbf{R}^3$ ):** A locally finite cell decomposition  $\mathcal{K}$  of  $X$  is called a flat origami if for an arbitrary closed curve  $\gamma$  in  $X$  such that  $\gamma$  does not pass through any 0 or 1-cell of  $\mathcal{K}$  and intersects 2-celles  $\sigma_1, \dots, \sigma_r$  of  $\mathcal{K}$  transversally in this order, the flat condition holds:

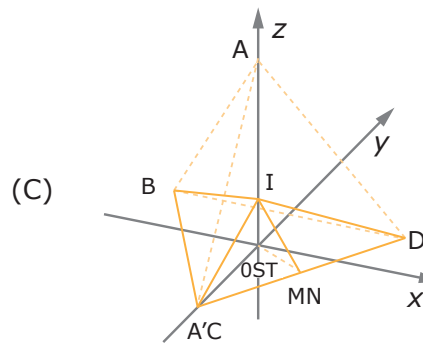
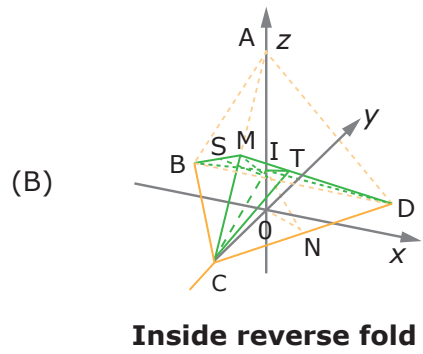
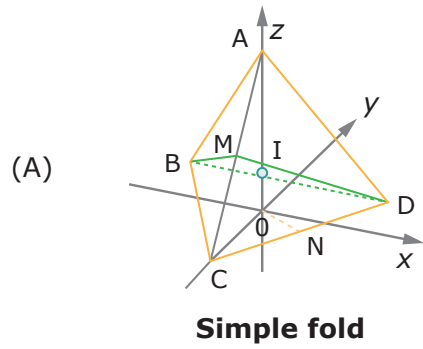
$$R(\sigma_1) \cdots R(\sigma_r) = \text{identity}.$$

Fig. 1.1, 1.2, 1.3 removed due to copyright restrictions.

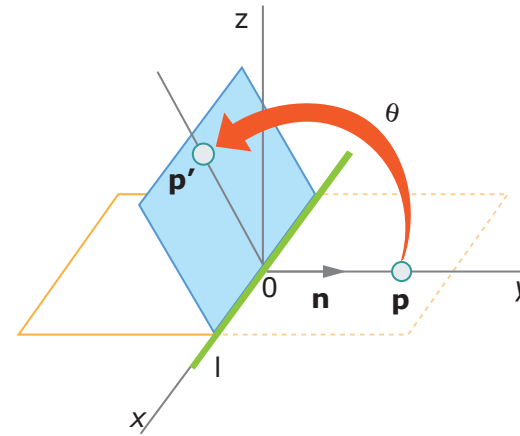
Refer to: Kawasaki, Toshikazu. "On High Dimensional Flat Origamis." *Proceedings of the First International Meeting of Origami Science and Technology* (1989): 131–41.

Read the abstract: Inoue, A., R. Itohara, et al. "[CG Image Generation of Four-Dimensional Origami.](#)"  
*The Journal of The Institute of Image Information and Television Engineers* 60 (2006):1630–47.

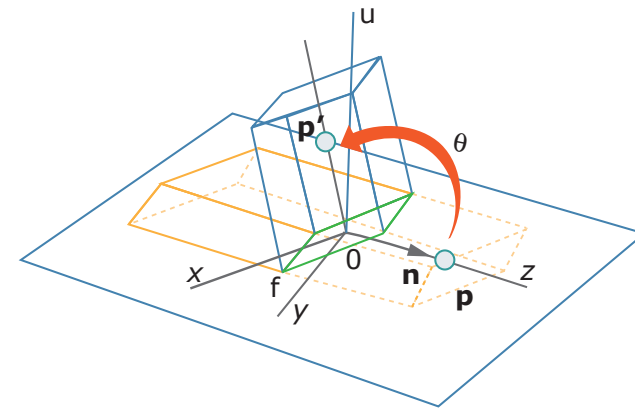
# Folding of Regular Tetrahedron



## Simple Fold



**(A) 3-D Origami**



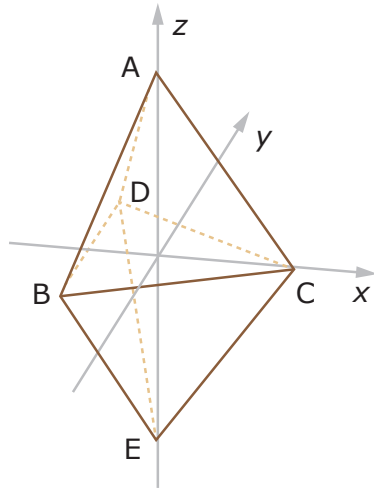
**(B) 4-D Origami**

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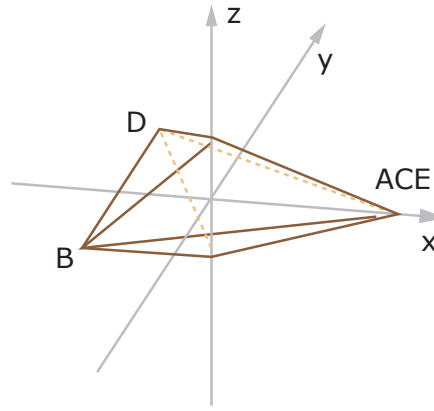
Refer to: Inoue, A., R. Itohara, K. Yajima, et al. "CG Image Generation of Four-Dimensional Origami." *The Journal of The Institute of Image Information and Television Engineers* 60 (2006): 1630-47.



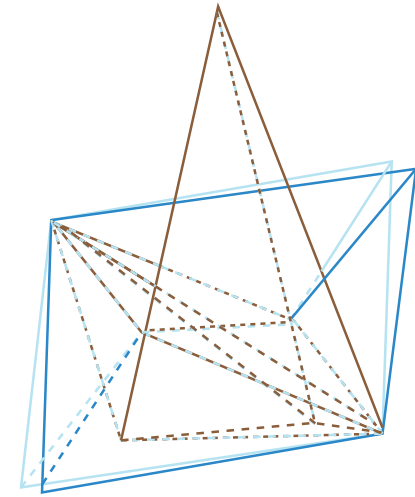
# Four-Dimensional Bird



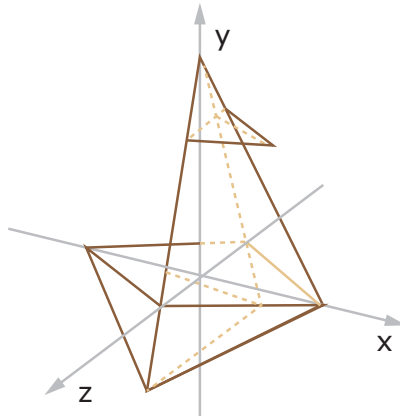
(A) Double tetrahedron



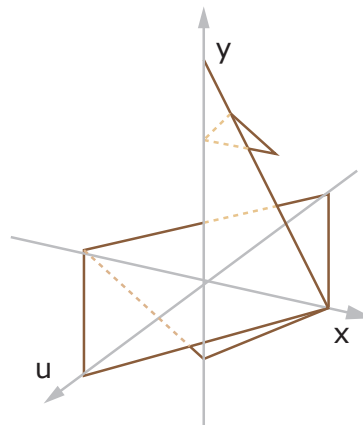
(B) Bird base



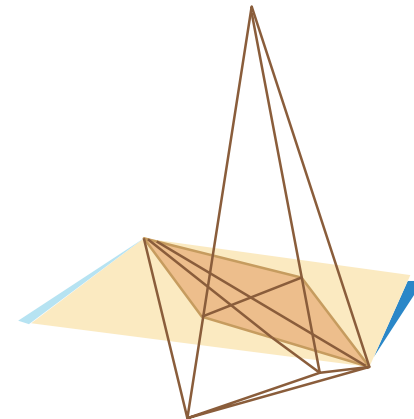
(A) Wire frame model



(C) Projection on  $u=0$



(D) Projection on  $z=0$



(B) Solid model

Image by MIT OpenCourseWare.

Refer to: Inoue, A., R. Itohara, K. Yajima, et al. "CG Image Generation of Four-Dimensional Origami." *The Journal of The Institute of Image Information and Television Engineers* 60 (2006): 1630-47.

**We've spent a good chunk of time talking about flat foldability. What is the significance to this? Why is so much work done coming up with proofs and algorithms regarding this?**



“Ralf Konrad's  
Rubik's Cube  
Tessellation”

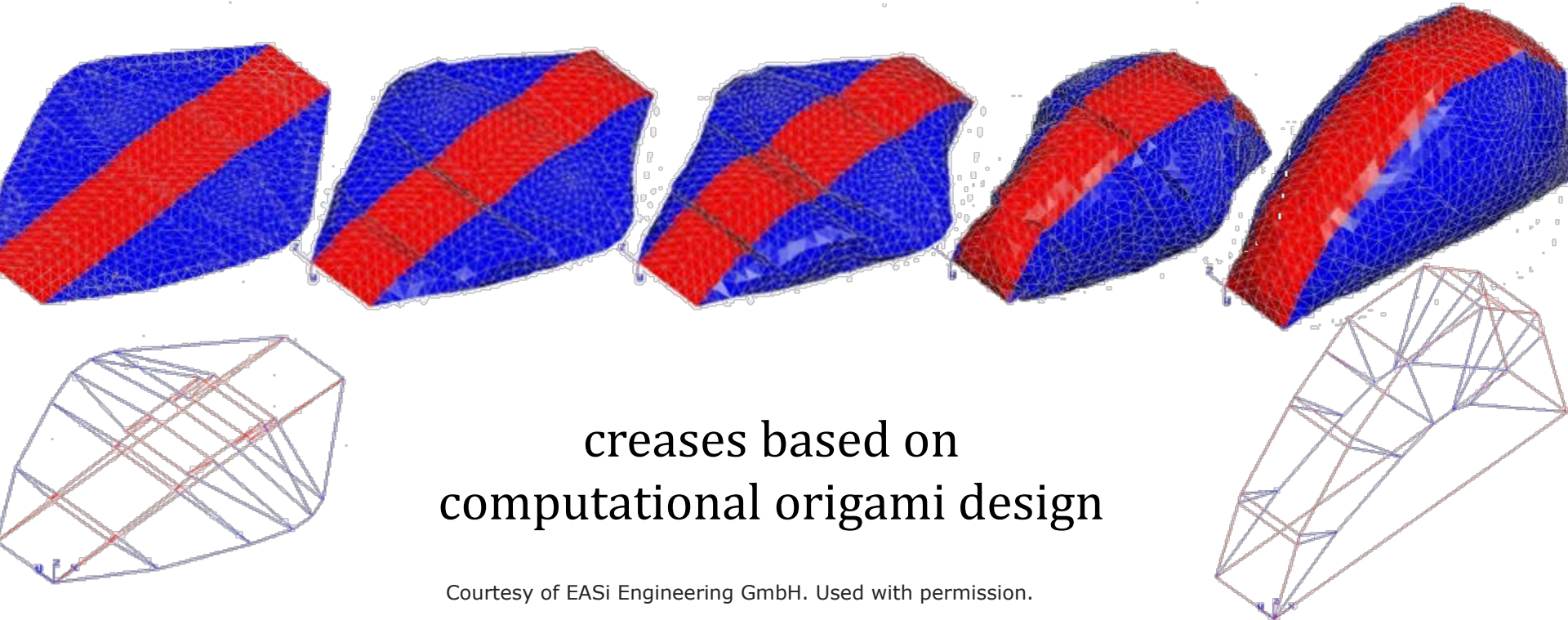
Jorge Jaramillo  
/ georigami

January 2007

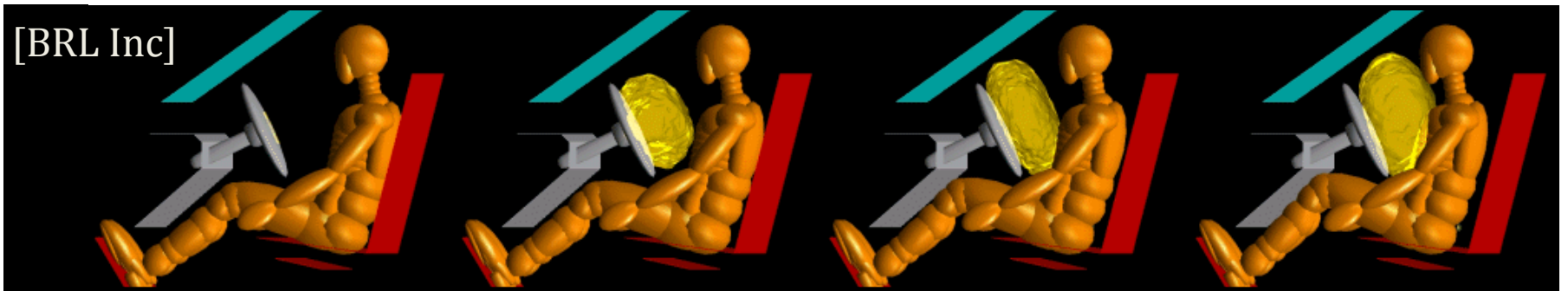
Photo courtesy of [georigami](#) on Flickr. Used with permission. Under CC-BY.

# Airbag Folding

[EASi Engineering]



[BRL Inc]



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# Generalization of Rigid Foldable Quadrilateral Mesh Origami

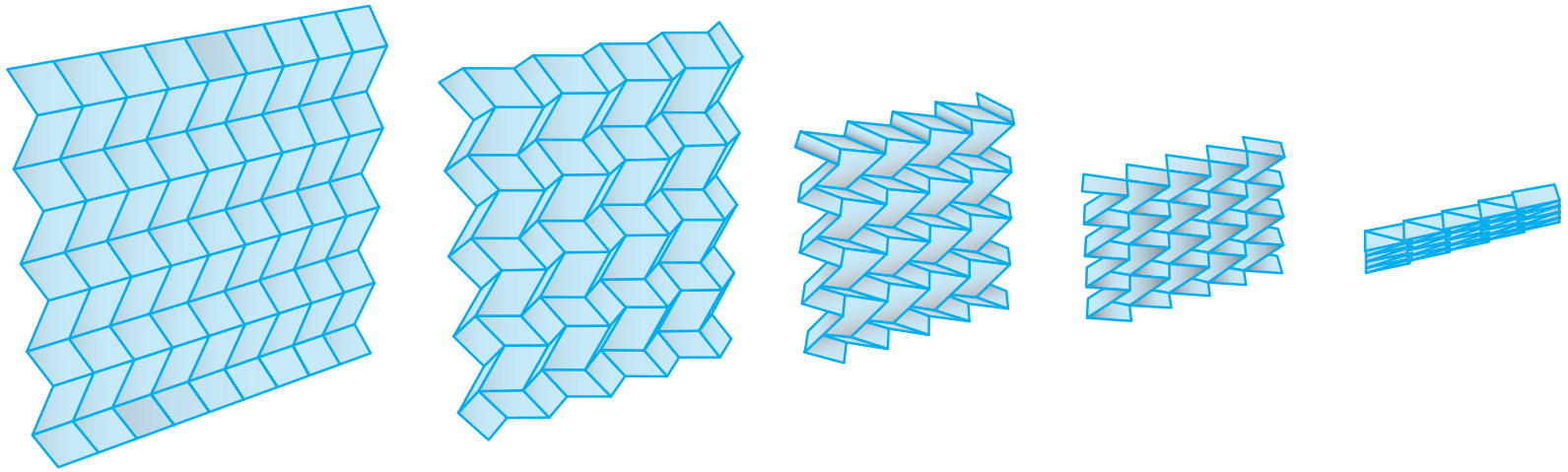
Tomohiro TACHI\*

\* The University of Tokyo

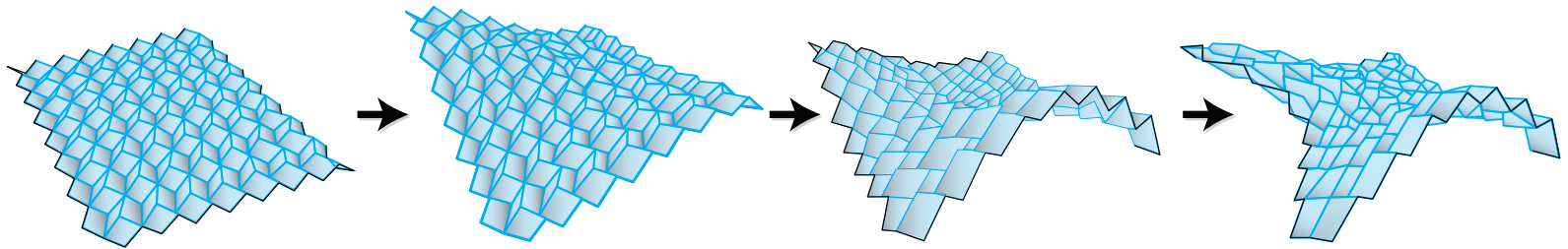
7-3-1 Hongo , Bunkyo-ku, Tokyo 113-8656, Japan

**Theorem 2** *Any flat-foldable planar-quad mesh origami has rigid-folding motion if and only if there exists a non-trivial valid state, i.e., every foldline is folded ( $\rho \neq 0$ ) but not completely folded ( $\rho \neq \pi, -\pi$ ).*

### Miura-ori



### Perturbation of Miura-ori



### Freeform Miura-ori

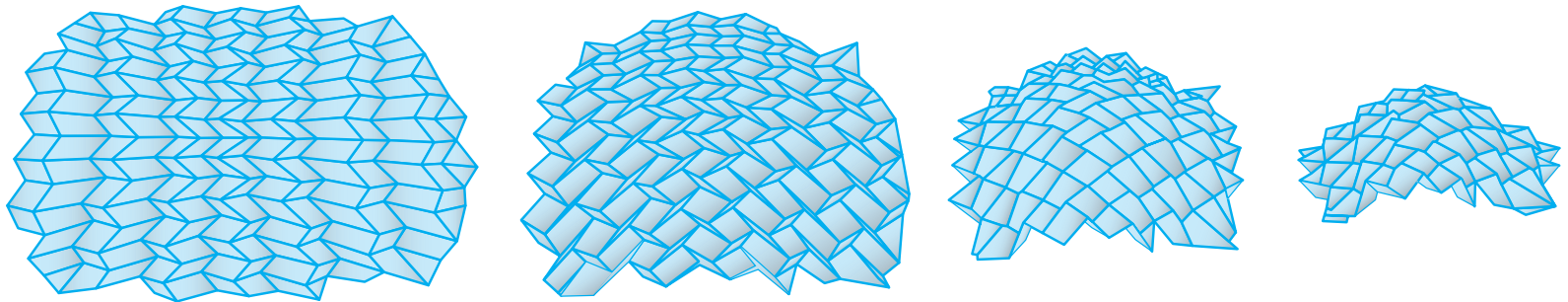


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Refer to: Tachi, Tomohiro. "Generalization of Rigid Foldable Quadrilateral Mesh Origami." *Proceedings of the International Association for Shell and Spatial Structures (IASS) Symposium 2009*.

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6.849 Geometric Folding Algorithms: Linkages, Origami, Polyhedra  
Fall 2012

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